# Spring Loaded Double Pantograph: A Robotic Mechanism for Safe Balance Training

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Abstract—A Spring Loaded Double Pantograph (SLDP) mechanism is presented for safe balance training in elderly individuals practicing Tai Chi exercises. As people age, maintaining balance becomes increasingly critical, yet fear of falling often prevents effective exercise, creating a counterproductive cycle that increases fall risk. This natural hesitation to push physical limits during solo practice highlights the need for reliable safety systems. This paper presents a mechanism that provides variable assistance through spring-loaded actuation, so that support and freedom of movement can be balanced in a way that is both effective and unobtrusive. Here, it will be shown that, although support and unrestricted movement are traditionally considered contradictory goals, the two can be achieved simultaneously through mechanical design and the level of assistance can be automatically regulated. In this system, the support mechanism can a) detect falls rapidly, b) provide up to 98.0% body weight support when needed, and c) remain imperceptible during normal exercise. First, the mechanical design principles and kinematic analysis of the double-pantograph structure are presented. Methods for experimental validation with 13 human subjects will be addressed, demonstrating the system's effectiveness through quantitative metrics of support forces, workspace utilization, and energy efficiency during simulated falls in Tai Chi movements.

# I. INTRODUCTION

As we age, maintaining balance becomes increasingly critical for independence and quality of life [4]. Regular balance training significantly reduces the risk of falling and improves mobility in older adults [44]–[46], with Tai Chi mind-body exercises [1]–[3] showing particularly strong evidence. However, many individuals, particularly those exercising alone, without the support of in-person trainers, may not reach the full potential of training due to fear of falling. This creates a counterproductive cycle - the fear of falling prevents effective challenge-based training, which in turn increases fall risk.

Imagine practicing challenging balance exercises with complete peace of mind - even as we age - knowing that an invisible safety net will catch you if you stumble, yet never



Fig. 1: Tai Chi expert <sup>1</sup> demonstrating traditional movements [39]. These movements illustrate the range of motion and support requirements that informed our system design and guided the development of the SLDP mechanism.

interfere with your natural movements. For older adults, this means pushing physical limits without the constant fear of falling. This seamless integration of human motion and robotic support represents a fundamental challenge in rehabilitation robotics: how do we create support systems that remain imperceptible during normal movement, yet provide instant protection when needed? Such a system could transform how aging individuals approach balance training, enabling more effective exercise programs and ultimately reducing fall risk in our growing elderly population.

Current robotic support systems face three key challenges: maintaining natural movement patterns, providing variable assistance based on user needs, and ensuring rapid response to potential falls. To address these challenges, we propose a Spring Loaded Double Pantograph (SLDP) mechanism that provides variable assistance to the user's movements and balance needs in real time. Unlike traditional systems, the SLDP allows for unrestricted movement in three dimensions while maintaining supportive capabilities.

The key contributions of this paper are:

- Mechanism Design: A Spring Loaded Double Pantograph (SLDP) mechanism, combining double-pantograph linkage with spring-loaded actuation to provide adaptive support while preserving natural movement patterns.
- 2) Physical Prototype: A physical system capable of supporting users up to 100 kg within a workspace of 0.4 to 1.1m radius and 128.9° arc.
- 3) Experimental Validation: Evaluation of the system with 13 human subjects performing Tai Chi exercises through simulated falls.

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 $<sup>1</sup>_{\mbox{Tai Chi https://sprinq-loaded-double-pentograph-robot.github.io/tai-chi/}$ 

#### II. RELATED WORK

#### A. Basic Mechanisms

The pantograph mechanism has a rich history in handling heavy loads while maintaining precision. Early applications in industrial cranes by Walter et al. [6] demonstrated its effectiveness in load manipulation, while Gostling's work [7] established fundamental principles for gravity compensation in pantograph-based systems. These early developments highlighted the mechanism's inherent mechanical advantage and workspace flexibility. Pioneering work by Hirose [11] in robotic locomotion further advanced the concept through 3D Cartesian coordinate pantograph mechanisms, demonstrating their capabilities for motion control. This work established fundamental principles of gravitationally decoupled actuation using pantograph structures, providing insights into mechanism design for complex spatial movements. Building on this, researchers explored pantograph applications in various domains - from large-scale construction manipulators [8] to precise surgical instruments [9]. Hirose's work focused primarily on single pantograph mechanisms for robotic manipulation and quadruped locomotion, without addressing human support systems. The mechanisms lacked the compliance needed for safe human interaction. Similarly, while industrial applications demonstrated the pantograph's load-bearing capabilities [6], they weren't designed for the dynamic and unpredictable nature of human movement support.

# B. Human Support Systems

Existing robotic support systems can be categorized into:

- Cable-Driven Support Systems: FLOAT [29] and ZeroG
  [30] use overhead cables to provide body weight support. While they offer more freedom than exoskeletons, they are typically limited to a fixed workspace and struggle with support across varied motion patterns.
- Balance-Assisting Wearable systems: Lighter systems like the BalanceAid [33] and the Smart Belt [34] provide sensory augmentation or minimal physical support. However, they may offer insufficient assistance for users with significant balance impairments.
- Soft Exosuits: More recent developments like the Soft Exosuit [35] [43] offer better compliance than rigid exoskeletons. However, current designs are limited in their ability to support three-dimensional movements and provide variable levels of assistance.
- Robotic Walker Assistants: Advanced robotic walkers such as as the Handle Anywhere Robot [25] and the Two-Body Robot [26] to provide body support and reconfigurable walkers as in [42] provide mobile support but typically restrict user arm movements and are not suitable for exercises that require unconstrained full-body motion.

These limitations stem from fundamental design approaches that prioritize either support or freedom of movement, but struggle to effectively balance both. Our proposed SLDP mechanism addresses these limitations by providing adaptive support while maintaining natural movements.

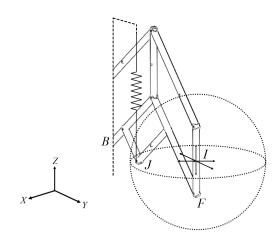


Fig. 2: 3D kinematic configuration of the SLDP mechanism showing the linkage arrangement.

# III. SYSTEM OBJECTIVES

Through observational study of Tai Chi movements [39] [40] [41] and expert demonstrations (Fig. 1), we identified core principles:

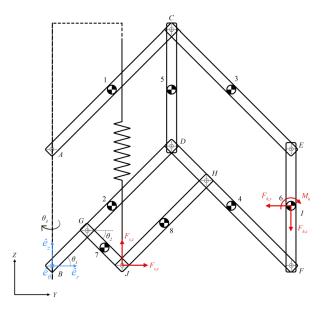
- The practitioner moved freely in all directions, demonstrating unrestricted natural movements
- The practitioner maintained balance by shifting weight between stances and providing appropriate self-support
- When teaching patients, a human assistant observed the practitioner's demonstrations while staying ready to catch them if they lost balance during practice

From these principles, we determined three system objectives for supporting elderly or physically impaired users during exercise:

- 1) Maintain Natural Movement: Enable unrestricted motion in three-dimensional space without constraining the user's movement patterns
- 2) Provide Adaptive Support: Deliver variable assistance that matches the user's changing support needs during weight shifts and transitions
- Fall Protection: Detect and respond rapidly to loss of balance while remaining unnoticeable during normal movement

# IV. MECHANISM

The Spring Loaded Double Pantograph (SLDP) mechanism, illustrated in Fig. 2, introduces our approach to adaptive support for human movements in three-dimensional space. This design combines a double-pantograph linkage with spring-loaded actuation at point J to support the payload at point I. The 3D configuration enables the end effector to move freely in X, Y, and Z axes while maintaining key geometric constraints, with points B, J and F remaining collinear throughout the motion. This design creates a spherical workspace that supports multi-planar movements essential for dynamic balance exercises such as Tai Chi.



| Nomenclature   |   |  |  |  |  |  |  |
|----------------|---|--|--|--|--|--|--|
| $\overline{g}$ | gravity vector                              |  |  |  |  |  |  |
| K              | spring stiffness parameter                  |  |  |  |  |  |  |
| $\overline{m}$ | counterweight mass                          |  |  |  |  |  |  |
| $M_h$          | joint reaction moment magnitude             |  |  |  |  |  |  |
| N              | Total number of mechanism Degrees of Freedo |  |  |  |  |  |  |
| $\omega$       | angular velocity                            |  |  |  |  |  |  |
| $F_h, z$       | human force in $\hat{e_z}$ direction        |  |  |  |  |  |  |
| $F_h, y$       | human force in $\hat{e_r}$ direction        |  |  |  |  |  |  |
| $F_s, z$       | spring force in $\hat{e_z}$ direction       |  |  |  |  |  |  |
| $F_s, y$       | spring force in $\hat{e_r}$ direction       |  |  |  |  |  |  |
| $L_2$          | link 2 length                               |  |  |  |  |  |  |
| $L_4$          | link 4 length                               |  |  |  |  |  |  |
| $L_6$          | link 6 length                               |  |  |  |  |  |  |
| $	heta_1$      | angle from horizontal to link 2             |  |  |  |  |  |  |
| $\theta_2$     | angle from horizontal to link 7             |  |  |  |  |  |  |
| $\theta_3$     | angle from Y axis to plane of mechanism     |  |  |  |  |  |  |

Fig. 3: Definition of coordinate systems and kinematic parameters with accompanying nomenclature

#### V. ANALYSIS

#### A. Kinematic Analysis

The kinematic diagram of the SLDP mechanism is illustrated in Figure 3. A key feature of the SLDP's design is the parallel arrangement of certain links - specifically, links 7, 4, and 3 are parallel to each other, as are links 2, 8, and 1. In this configuration, external forces acting at joints J and I are denoted in red, representing the interaction points with the user and the environment.

We introduce a rotating reference frame at point B. In this frame, unit vectors  $\hat{e}_r$ ,  $\hat{e}_\theta$ , and  $\hat{e}_z$  move with the mechanism, with  $\hat{e}_\theta$  always remaining orthogonal to link 2 and rotating at a constant angular velocity  $\dot{\theta}_3$ .

We derive an expression for the position vector of Point I (the end effector) relative to Joint B. Using the geometry of the linkage, we obtain:

$$\vec{r}_I = L_2 \begin{pmatrix} \cos \theta_1 \\ \sin \theta_1 \end{pmatrix} + L_4 \begin{pmatrix} \cos \theta_2 \\ -\sin \theta_2 \end{pmatrix} + \frac{L_6}{2} \begin{pmatrix} 0 \\ 1 \end{pmatrix} \quad (1)$$

In this expression,  $L_2$  and  $L_4$  represent the lengths of their respective links, while  $\theta_1$  and  $\theta_2$  are the angles these links make with the horizontal. The term  $\frac{L_6}{2}$  accounts for the half-length of link 6, which connects to the end effector.

To analyze the velocity of the end effector, we first consider the case where  $\dot{\theta}_3=0$ , effectively analyzing the motion in the YZ plane. Differentiating Equation (1) with respect to time yields:

$$\vec{v}_I' = \begin{bmatrix} -L_2 \sin \theta_1 & -L_4 \sin \theta_2 \\ L_2 \cos \theta_1 & -L_4 \cos \theta_2 \end{bmatrix} \begin{pmatrix} \dot{\theta}_1 \\ \dot{\theta}_2 \end{pmatrix}$$
(2)

This equation expresses the end effector velocity,  $\vec{v}_I'$ , as a function of the angular velocities  $\dot{\theta}_1$  and  $\dot{\theta}_2$ , with the matrix representing the Jacobian for this two-dimensional case.

To extend our analysis to three dimensions, we introduce rotation around the Z-axis. Setting  $\dot{\theta}_3 = \omega \hat{e}_z$  (with  $\dot{\omega} = 0$ ) and differentiating Equation (1) again, we obtain:

$$\vec{v}_I = \begin{bmatrix} -L_2 \sin \theta_1 & -L_4 \sin \theta_2 & 0\\ 0 & 0 & -L_2 \cos \theta_1\\ & -L_4 \cos \theta_2 \end{bmatrix} \begin{pmatrix} \dot{\theta}_1\\ \dot{\theta}_2\\ \dot{\theta}_3 \end{pmatrix} \quad (3)$$

This three-dimensional velocity equation now includes components in the  $\hat{e}_r$ ,  $\hat{e}_\theta$ , and  $\hat{e}_z$  directions, describing the motion of the end effector in 3D space.

The workspace of the SLDP is defined by the ranges of the angles  $\theta_1$  and  $\theta_2$ . Both angles are constrained to the domain  $[0,\pi]$ . These constraints arise from the physical limitations of the mechanism:

$$0 < \theta_1, \theta_2 < \pi \tag{4}$$

It's important to note that these workspace calculations do not account for the physical constraint imposed by the spring. In practice, an additional constraint would be applied such that:

$$\theta_1 + \theta_2 < \pi \tag{5}$$

This constraint is necessary because the spring only engages when the end effector reaches the horizontal formed by the y-axis. At the point where  $\theta_1 + \theta_2 = \pi$ , the end effector would lie on the y-axis, defining the limit of the mechanism's range of motion.

## B. Workspace Analysis

We analyzed the SLDP mechanism's workspace through both simulation and experimental validation. The simulated analysis, shown in Fig. 4, maps the workspace by varying

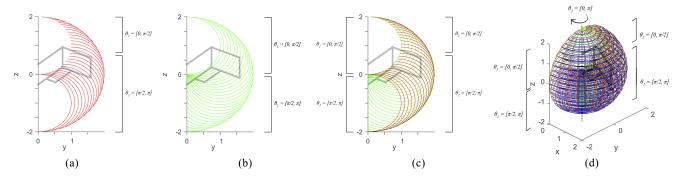


Fig. 4: Simulated workspace for the end effector. Subfigure (a) demonstrates the sweeps of the end effector in the yz-plane as a function of  $\theta_1$ . A singular sweep represents the position of the end effector as a function of  $\theta_1$  in the domain  $[0,\pi]$  while  $\theta_2$  remains at a set value within the range  $[0,\pi]$ . We form the whole workspace when we iterate through discrete values of  $\theta_2$  in a linearly spaced set in the domain  $[0,\pi]$ . Subfigure (b) demonstrates the sweeps of the end effector in the yz-plane as a function of  $\theta_2$ . The process is repeated with  $\theta_1$  remaining at a set value within the range  $[0,\pi]$ . While  $\theta_2$  continuously sweeps through the domain  $[0,\pi]$ . Subfigure (c) demonstrates the entire workspace of the end effector in the two-dimensional yz-plane as both a function of  $\theta_1$  and  $\theta_2$ . Subfigure (d) demonstrates the 3D workspace of the end effector as a function of  $\theta_1$ ,  $\theta_2$ , and  $\theta_3$ . A singular sweep in the xy-plane (shown in blue) represents the position of the end effector as a function of  $\theta_3$  in the domain  $[\pi/2, -\pi/2]$  while  $\theta_1$  and  $\theta_2$  remain at set values.

joint angles  $\theta_1$  and  $\theta_2$  in the YZ-plane, and rotating through  $\theta_3$  [ $-\pi/2$ ,  $\pi/2$ ] to generate the full three-dimensional spherical workspace. The simulations reveal that the SLDP mechanism achieves a spherical workspace capable of supporting multi-planar movements, with the end effector able to reach points within a radius of 0.4 to 1.1m and sweep through  $128.9^{\circ}$  arc - sufficient range for typical Tai Chi exercises.

## C. Static Analysis

The primary external forces acting on the system are the human interaction force  $(F_{h,z})$  at point I and the spring force  $(F_{s,z})$  at point J (see Fig. 3). Due to the double-pantograph geometry and parallel link arrangements, these forces are coupled through a mechanical advantage relationship:

$$F_{s,z} = \alpha F_{h,z} \tag{6}$$

where  $\alpha$  is the mechanical advantage factor determined by the mechanism's configuration. This relationship ensures that the spring provides proportional support based on the user's needs, with the support force automatically adjusting as the configuration changes.

The static equilibrium of the system is maintained through a network of internal forces transmitted through the parallel linkages, with the spring force effectively counterbalancing external loads while maintaining system stability. At joint J where the spring force is applied:

$$F_{s,z} + T_7 \sin \theta_2 + T_8 \sin \theta_1 = 0 \tag{7}$$

The complete static analysis, including detailed force balance equations for all links and joints, is provided in our online appendix <sup>2</sup>.

# VI. SYSTEM



Fig. 5: Computer-aided design (CAD) model showing the SLDP system with support structure, mechanical linkages, and instrumentation placements <sup>3</sup>. The model illustrates key components including the double-pantograph mechanism, spring loading system, and sensor locations. A physical implementation of this design is shown in Figure 6.

Figure 6 shows the fabricated SLDP mechanism and its supporting hardware. A column-type load cell is placed on the wire supporting the system in order to measure the load applied. Three encoders are placed at joints B and J on the XZ-plane, as well as the XY-plane on at joint B to observe  $\theta_1$ ,  $\theta_2$ , and  $\theta_3$ . The end effector at joint I attaches to the human subject via a swivel and harness so that the user can maintain full freedom of motion.

The design process began with Computer-aided design (CAD) modeling, as shown in Figure 5, which enabled optimization of joint mechanisms, sensor placements, and safety features before physical construction. We utilized

<sup>2</sup> Static https://spring-loaded-double-pentograph-robot.github.io/static-analysis/

<sup>3</sup> Design https://spring-loaded-double-pentograph-robot.github.io/design/

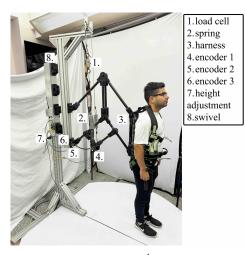


Fig. 6: Physical implementation <sup>4</sup> of the SLDP mechanism showing a user testing the system. Mechanical components and sensing instrumentation are annotated.

carbon fiber tubes for the primary linkages due to their exceptional strength-to-weight ratio. The main support links  $(L_1,\,L_2,\,L_3,\,L_4)$  measure 441 mm in length with a 30 mm diameter. The end effector link  $(L_6)$ , measuring 322 mm, was specially reinforced to handle direct user interactions.

Custom aluminum joint housings and precision ball bearings were integrated at all rotating joints to ensure smooth, low-friction operation. The links are connected through custom-made FDM 3D printed parts with a micro carbon fiber-filled nylon and solid infill to support large payloads.

| Maximum Payload (kg)    | 100   |
|-------------------------|-------|
| Maximum Radius (m)      | 1.1   |
| Minimum Radius (m)      | 0.4   |
| Maximum Sweep Angle (°) | 128.9 |
| Spring Constant (kN/m)  | 73    |
| Overall Mass (kg)       | 11.3  |

TABLE I: Mechanical System Parameters

We installed a high-precision column-type load cell with 700kg capacity and a digital amplifier with 0.1 N resolution to measure support forces, and three rotary shaft encoders with 14-bit resolution and quadrature encoding strategically placed to monitor the critical angles  $\theta_1$ ,  $\theta_2$ , and  $\theta_3$ .

Our prototype's key mechanical parameters are summarized in Table I. The system supports a maximum payload of 100 kg while maintaining a relatively light overall mass of 11.3 kg. The mechanism operates within a workspace defined by a maximum radius of 1.1 m and a vertical range from 0.2 m to 1.8 m above ground level. The spring system, tuned with an effective constant of 73 kN/m, provides responsive support with less than 100 ms reaction time while maintaining position accuracy within ±2 mm at the end effector.

For human interface, we attached an ergonomic harness at joint I. The harness provides adjustable straps and quickrelease mechanisms that distribute support forces throughout the upper body while allowing natural arm and torso movements.

#### VII. EXPERIMENTATION

We conducted human subject testing to evaluate the effectiveness of the SLDP mechanism in providing support during Tai Chi exercises. The study protocol was approved by the Institutional Review Board (IRB Protocol #2212000845R001).

## A. Experimental Setup

The SLDP mechanism was equipped with three encoders monitoring joint angles  $(\theta_1, \theta_2, \theta_3)$  and a load cell measuring vertical support force. Ground reaction forces were measured using force-sensitive insole resistors attached to the subjects' shoes. The data acquisition system sampled all sensors at 1 kHz, while a synchronized video recording system captured movement data for detailed analysis.

# B. Subject Demographics

Thirteen subjects (8 male, 5 female) participated in the study, aged 18-35 years with mean weight  $64 \pm 8$  kg and height range 165-180 cm. The participants represented varying levels of Tai Chi experience, with two each at beginner, intermediate, and advanced levels. None had prior balance impairments.

# C. Experimental Protocol

Each subject performed three 60-second trials comprising three components. First, subjects executed standard Tai Chi movements including Wave Hands Like Clouds, Grasp Bird's Tail, and Single Whip. Second, they performed intentional balance perturbations consisting of two to three staged falls per trial in various directions (forward, backward, lateral), with timing unknown to the system. Finally, subjects completed free-form movements within the workspace.

# VIII. EVALUATION

#### A. Metrics

We define the following metrics in order to evaluate the performance:

## 1) SLDP Support Fraction is defined as:

$$R_{SLDP} := \frac{F_{s,z}}{\alpha W_h} \tag{8}$$

where  $W_h$  is the weight of the human,  $F_{s,z}$  is the measured restoring spring force, and  $\alpha$  is the mechanical advantage factor of the pantograph. This provides a dimensionless measure of the fraction of user weight supported by the system during a fall event.

## 2) Foot Support Fraction is defined as:

$$R_{\text{Foot}} := \frac{\int_{A_L} P_L \, dA + \int_{A_R} P_R \, dA}{W_h} \tag{9}$$

where  $P_L$  and  $P_R$  are the current foot pressure values from the left and right insole sensor respectively;  $A_L$  and  $A_R$  are the area of the left and right foot respectively.

<sup>4</sup> Fabrication https://spring-loaded-double-pentograph-robot.github.io/fabrication/

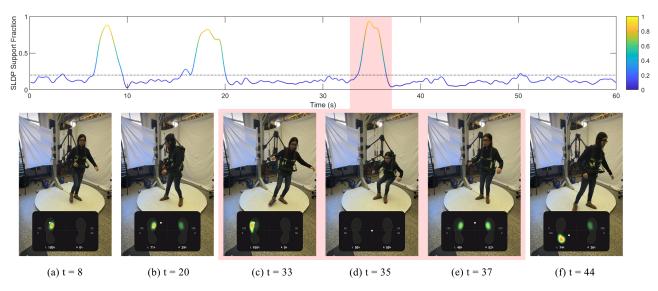


Fig. 7: The figure shows the SLDP Support Fraction (described in section VIII) over a period of 60 seconds. Below the force graph is a series of images of the subject performing Tai Chi exercises. Each image also contains a visual of the weight distribution and force applied to the feet from the insole sensor attached to the user's feet. Three large spikes in support appear on the graph when the subject trips and falls. The highlighted red region shows a successive fall and recovery. In frame (d), as the subject falls, the force and weight distributed to the feet drop as seen on the weight distribution map. The system supports the subject's weight during this period as demonstrated by the spike at t=35. When the subject picks herself up in frame (e), the force into the feet increases. The system provides less support now that the subject is standing independently, as shown by the drop in support at t=37. Frame (a), (b), and (f) demonstrate the subject performing regular exercises without any falling or tripping. One can observe that often an increase in force on the system results in less weight on the feet, while an increase in pressure on the feet results in less force on the SLDP system. The full video of this user session with detailed results can be found in our online appendix  $^5$ .

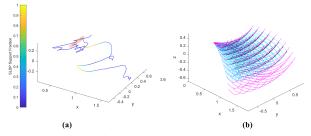


Fig. 8: (a) End effector path of the system. The graph demonstrates the support fraction applied at each location of the end effector along the path with the orange regions showing higher support fraction and blue showing low force applied. Notice the highlighted region in red corresponds to the highlighted region of Figure 7 in which a fall is analyzed. (b) Workspace explored during user trial. The minimum and maximum angles were determined and used.

- 3) **Range of Motion** The total angle swept by the user in the xy-plane, as measured by  $\theta_3$ . A larger angle (within the actual workspace) indicates the user's motion was unrestricted and fulfillment of our first system objective.
- 4) Max Fall Distance The maximum distance in the z-

direction which the end effector was displaced during a fall. A smaller value demonstrates that the system adequately prevented a large vertical displacement and upheld the user during a fall.

5) Fall Detection A fall event was identified when:

$$Fall = \begin{cases} 1, & \text{if } (R_{SLDP} > \mu_R + 2\sigma_R) \\ & \wedge (\frac{dR}{dt} > \beta) \wedge (P_f < \gamma P_0) \\ 0, & \text{otherwise} \end{cases}$$
 (10)

where  $F_v$  is vertical force measured at SLDP end effector;  $P_f$  is current foot pressure from insole sensors;  $P_0$  is baseline standing foot pressure;  $\mu_R$  is the mean of  $R_{SLDP}$ ;  $\sigma_R$  is the standard deviation of  $R_{SLDP}$ ;  $\beta=200$  N/s (force rate threshold);  $\gamma=0.5$  (foot pressure reduction threshold).

False positive mitigation used temporal validation and joint angle tracking:

$$\mbox{ValidFall} = \mbox{Fall} \wedge \begin{cases} 1, & \mbox{if } (t > t_{\min}) \wedge (\Delta \theta > \theta_{\text{thresh}}) \\ 0, & \mbox{otherwise} \end{cases} \label{eq:ValidFall}$$

where:  $t_{\rm min}=100{\rm ms}$  (minimum duration);  $\Delta\theta=\sqrt{(\theta_1-\theta_{1,0})^2+(\theta_2-\theta_{2,0})^2}; \; \theta_{\rm thresh}=15$  (angle deviation threshold); and  $\theta_{1,0},\theta_{2,0}$  are baseline standing angles.

 $<sup>\</sup>mathbf{5}_{\mathbf{Users:}\,\mathbf{https://spring-loaded-double-pentograph-robot.github.io/user-sessions/}$ 

### B. Results and Analysis

We evaluated the performance of the SLDP mechanism in the physical system through experimental trials with 13 users, analyzing its performance against our three system objectives (originally outlined in Section III):

- 1) maintaining natural movement patterns by allowing unrestricted motion in 3D space
- 2) providing adaptive assistance based on user needs
- 3) ensuring rapid fall detection and prevention

Range of Motion Analysis The SLDP mechanism allowed users to move without impedance within workspace. Figure 9 demonstrates the experimental workspace formed from all user trials. The range of the parameters are described in Table II. The agreement of simulated (Fig. 4) and experimental workspace (Fig. 9) indicate that users moved freely satisfying the first system objective.

Support Analysis The SLDP mechanism demonstrated strong ability to variably support user weight across all testing. Figure 10 compares the user weight to the peak forces measured during fall events. The slope of the curve fit coupled with the mechanical advantage  $\alpha=1.08$  provides a metric for what fraction of user weight is being supported. We determine that the system supports an average of 71.48% of a user's weight across all falls. The system also demonstrated a robust performance in preventing large vertical displacements during a fall event. Figure 10 compares the fall distance to user weight. The linear fit produces small parameters, indicating minimal vertical displacement even at high loads. These mechanism analytics and Figure 7 support the fulfillment of our second system objective.

Fall Analysis Throughout the experimental trials, the SLDP mechanism demonstrated robust fall detection capabilities. By combining load cell measurements with our detection criteria (Equation 10), we evaluated the system's detection accuracy against visually observed falls. The results, presented as a confusion matrix in Figure 11, show that across all 13 trials, the system identified 33 out of 38 actual falls, while generating 8 false positive detections. This 86.8% detection rate with a moderate false positive ratio indicates that the mechanism achieves our third objective of reliable fall protection, though with a conservative bias toward overdetection to user safety.

# IX. LIMITATIONS

- Current passive design lacks adaptability to different users and movement patterns. Future integration of active control with passive compliance and user-specific learning algorithms would enable uniform force distribution and real-time adaptation.
- Fixed workspace (0.4-1.1m radius and 128.9° angle) and constant spring stiffness limit system flexibility. Implementation of modular links and variable stiffness springs would enhance adaptability.
- The current 100 ms latency is inadequate for rapid fall prevention. Integration of IMU sensors and machine learning algorithms would enable anticipatory support.

 Experimental Validation included limited testing on only 13 subjects (age 18-35). Expanded trials across diverse populations and long-term studies is needed to validate system effectiveness.

|    |     | $\theta_1$ (rad) | $\theta_2$ (rad) | $\theta_3$ (rad) | x (m) | y (m) | z (m) |
|----|-----|------------------|------------------|------------------|-------|-------|-------|
| M  | in. | 0                | 0                | -1.09  rad       | 0.40  | 0.40  | -0.25 |
| Ma | ax. | 0.97 rad         | 1.09 rad         | 1.18 rad         | 1.10  | 1.10  | 0.27  |

TABLE II: Range of geometric parameters for SLDP mechanism across all user trials.

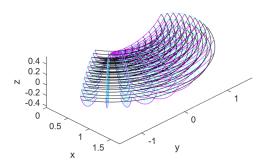


Fig. 9: Experimental workspace volume across all user trials. The minimum and maximum for  $\theta_1, \theta_2$  and  $\theta_3$  were measured and used to form the actual workspace volume.

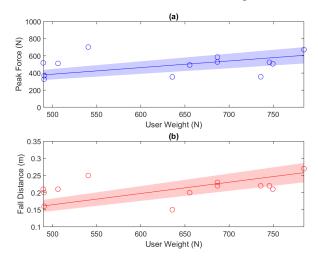


Fig. 10: Scatter plots of the different users' weight to peak force and max fall distance with proportional fit  $y=Ax, A=0.77\pm0.12\frac{N}{N}$  for Subplot (a) and  $A=0.000329\pm0.000036\frac{m}{N}$  for Subplot (b) applied. The shaded region described the 95% confidence region for the fit.

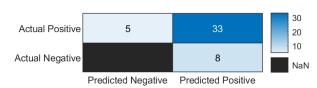


Fig. 11: Confusion matrix of the fall detection abilities of the system. 33 of the 38 falls were recognized, while 8 false positives were recorded. The true negative is left null due to the fact that "not falling" cannot be a recorded event.

## X. CONCLUSION

This paper addresses the critical challenge of providing support for dynamic exercises in aging individuals, specifically focusing on maintaining natural movement patterns, proportional assistance, and rapid fall response. We propose a Spring Loaded Double Pantograph (SLDP) mechanism that combines a double-pantograph linkage with springloaded actuation to deliver adaptive support across a threedimensional, spherical workspace. The mechanism demonstrated on a physical prototype performed robustly during user testing with Tai Chi Activity and staged falls; the mechanism supported 71.48% of user weight during fall events. Future developments incorporating active control and advanced sensing could further enhance the system's capabilities. The SLDP mechanism's principles could also extend beyond Tai Chi exercises to various applications in rehabilitation, elderly care, and general exercise support.

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